

Cambridge International AS Level

MATHEMATICS
Paper 2 Pure Mathematics 2
MARK SCHEME
Maximum Mark: 50

Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.

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Generic Marking Principles

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

GENERIC MARKING PRINCIPLE 1:

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:

Marks awarded are always whole marks (not half marks, or other fractions).

GENERIC MARKING PRINCIPLE 3:

Marks must be awarded positively:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently, e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

© UCLES 2022 Page 2 of 11

Math	Mathematics Specific Marking Principles				
1	Unless a particular method has been specified in the question, full marks may be awarded for any correct method. However, if a calculation is required then no marks will be awarded for a scale drawing.				
2	Unless specified in the question, answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected.				
3	Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.				
4	Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored (isw).				
5	Where a candidate has misread a number in the question and used that value consistently throughout, provided that number does not alter the difficulty or the method required, award all marks earned and deduct just 1 mark for the misread.				
6	Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.				

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Mark Scheme Notes

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

Types of mark

- Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
- **B** Mark for a correct result or statement independent of method marks.
- DM or DB When a part of a question has two or more 'method' steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly, when there are several B marks allocated. The notation DM or DB is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
 - FT Implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only.
- A or B marks are given for correct work only (not for results obtained from incorrect working) unless follow through is allowed (see abbreviation FT above).
- For a numerical answer, allow the A or B mark if the answer is correct to 3 significant figures or would be correct to 3 significant figures if rounded (1 decimal place for angles in degrees).
- The total number of marks available for each question is shown at the bottom of the Marks column.
- Wrong or missing units in an answer should not result in loss of marks unless the guidance indicates otherwise.
- Square brackets [] around text or numbers show extra information not needed for the mark to be awarded.

© UCLES 2022 Page 4 of 11

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Abbreviations

AEF/OE Any Equivalent Form (of answer is equally acceptable) / Or Equivalent

AG Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)

CAO Correct Answer Only (emphasising that no 'follow through' from a previous error is allowed)

CWO Correct Working Only

ISW Ignore Subsequent Working

SOI Seen Or Implied

SC Special Case (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the

light of a particular circumstance)

WWW Without Wrong Working

AWRT Answer Which Rounds To

© UCLES 2022 Page 5 of 11

Question	Answer	Marks	Guidance
1(a)	State or imply equation is $\ln y = (2x - a) \ln 4$	B1	OE. Do not condone poor use of brackets.
	State gradient is 2ln4 and confirm ln16	B1	AG – necessary detail needed
		2	
1(b)	Substitute for $\ln y$ and attempt value of a	M1	Allow if $\ln y = 2x - a \ln 4$
	Obtain $a = 15$	A1	Integer answer required, but condone 15.0
		2	

Question	Answer	Marks	Guidance
2(a)	Attempt to express left hand side of the equation in terms of $\sin \theta$ and $\cos \theta$	M1	with at least two of the terms correct and no missing θ s Condone use of x instead of θ
	Obtain $7\sin^2\theta + 4\cos^2\theta - 13\sin\theta [= 0]$	A1	SOI, OE
	Obtain $3\sin^2\theta - 13\sin\theta + 4 = 0$	A1	Allow if missing θ s are recovered SC Allow full marks for $3\sin\theta - 13 + \frac{4}{\sin\theta} = 0$ Must be in terms of θ for final A mark
		3	

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Question	Answer	Marks	Guidance
2(b)	Attempt solution of 3-term quadratic equation for $\sin \theta$	M1	
	Obtain $\sin \theta = \frac{1}{3}$ and hence 19.5	A1	or greater accuracy
	Obtain second value 160.5	A1	or greater accuracy; and no other values within the given range FT on 180° – their 19.5°
		3	

Question	Answer	Marks	Guidance
3(a)	Attempt to find x-value from $3\sin x - 3\sin 2x = 0$ using identity for $\sin 2x$	M1	
	Obtain at least $\cos x = \frac{1}{2}$	A1	
	Obtain $\frac{1}{3}\pi$	A1	SC B3 can be spotted from $\sin x = \sin 2x$
		3	
3(b)	Integrate to obtain form $k_1 \cos x + k_2 \cos 2x$	*M1	non-zero constants k_1 , k_2 M0 for $3\cos x \pm 6\cos 2x$
	Obtain correct $-3\cos x + \frac{3}{2}\cos 2x$	A1	
	Attempt value of integral using their lower limit (in radians) and π correctly	DM1	Allow one sign error
	Obtain $\frac{27}{4}$	A1	OE
		4	

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Question	Answer	Marks	Guidance
4	Use product rule to differentiate x^2y	*M1	There must be evidence of implicit differentiation
	Obtain correct $2xy + x^2 \frac{dy}{dx}$	A1	
	Obtain $\left[2xy + x^2 \frac{dy}{dx} + \right] 6y^2 \frac{dy}{dx} = 0$	*B1	
	Substitute $x = 4$, $y = 2$ to find value of $\frac{dy}{dx}$	DM1	dependent on at least one term involving $\frac{dy}{dx}$
	Obtain $-\frac{2}{5}$	A1	SOI, OE
	Attempt equation of normal passing through (4, 2)	M1	with numerical gradient correctly obtained from the negative reciprocal of <i>their</i> derivative
	Obtain 5x - 2y - 16 = 0	A1	
		7	

Question	Answer	Marks	Guidance
5(a)	Draw correct sketch of $y = 5 - 2x $	*B1	with vertex on positive <i>x</i> -axis
	Draw correct sketch of $y = 3 \ln x$	*B1	
	Indicate the two roots either on the diagram or by a statement	DB1	
		3	

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Question	Answer	Marks	Guidance
5(b)	State $2x - 5 = 3 \ln x$ and rearrange to confirm $x = 2.5 + 1.5 \ln x$	B1	AG – necessary detail needed
		1	
5(c)	Consider sign of $x - 2.5 - 1.5 \ln x$, or equivalent, for 4.5 and 5.0	M1	
	Obtain -0.25 and 0.08 or equivalents and justify conclusion	A1	AG – necessary detail needed
	Alternative method for question 5(c)		
	Consider sign of $ 5-2x -3\ln x$, or equivalent, for 4.5 and 5.0	M1	
	Obtain -0.51 and 0.17 or equivalents and justify conclusion	A1	AG – necessary detail needed
		2	
5(d)	Use iteration process correctly at least once	M1	
	Obtain final answer 4.88	A1	Answer required to exactly 3 s.f.
	Show sufficient iterations to 5 s.f. to justify answer or show sign change in interval [4.875, 4.885]	A1	
		3	

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Question	Answer	Marks	Guidance
6(a)	Use quotient rule (or equivalent) to find first derivative	*M1	Condone poor use of brackets if recovered later
	Obtain $\frac{18e^{2x}(e^x - 1) - e^x(9e^{2x} + 16)}{(e^x - 1)^2}$	A1	OE
	Equate first derivative to zero and attempt factorisation	DM1	Need to be working with $9e^{3x} - 18e^{2x} \pm 16e^x = 0$
	Obtain $e^x (3e^x - 8)(3e^x + 2) = 0$	A1	AG – necessary detail needed SC B3 If numerator is in incorrect order and given result is obtained. SC B3 If denominator is not squared and given result is obtained.
		4	
6(b)	Observe, using given result from part (a), at some stage, $e^x \ne 0$ and $3e^x + 2 \ne 0$ and hence one stationary point	B1	Allow if discounted by crossing through OE
	Attempt exact solution for x and for y	M1	
	Obtain $x = \ln(\frac{8}{3})$ or exact equivalent	A1	
	Obtain $y = 48$	A1	Not from a rounded decimal
		4	

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Question	Answer	Marks	Guidance
7(a)	Carry out algebraic long division at least as far as $2x^2 + kx$	M1	
	Obtain quotient $2x^2 + x + a - 2$	A1	
	Confirm remainder is 4	A1	AG – necessary detail needed SC B1 for use of remainder theorem to obtain 4
		3	
7(b)	Identify integrand as $2x^2 + x + a - 2 + \frac{4}{x+2}$	B1 FT	Following their quotient, may be implied
	Integrate to obtain at least 2 terms from the form of $k_1x^3 + k_2x^2 + k_3\ln(x+2)$	M1	for non-zero k_1, k_2, k_3
	Obtain correct $\frac{2}{3}x^3 + \frac{1}{2}x^2 + ax - 2x + 4\ln(x+2)$	A1	
	Apply limits correctly and attempt correct process to find a or b	M1	Must have the correct form
	Obtain $-\frac{8}{3} + 2a = \frac{22}{3}$ or equivalent and hence $a = 5$	A1	
	Obtain $4 \ln 3$ and hence $b = 81$	B1	
		6	

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